

Identifying different stacking sequences in few-layer CVD-grown MoS₂ by low-energy atomic-resolution scanning transmission electron microscopy

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Atomically thin MoS₂ grown by chemical vapor deposition (CVD) is a promising candidate for next-generation electronics due to inherent CVD scalability and controllability. However, it is well known that the stacking sequence in few-layer MoS₂ can significantly impact electrical and optical properties. Herein we report different intrinsic stacking sequences in CVD-grown few-layer MoS₂ obtained by atomic-resolution annular-dark-field imaging in an aberration-corrected scanning transmission electron microscope operated at 50 keV. Trilayer MoS₂ displays a new stacking sequence distinct from the commonly observed 2H and 3R phases of MoS₂. Density functional theory is used to examine the stability of different stacking sequences, and the findings are consistent with our experimental observations.

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I. INTRODUCTION

Atomically thin molybdenum disulfide (MoS₂) has recently attracted significant attention due to its novel physical and electrical properties. Single-layer MoS₂ (extracted from naturally occurring 2H-phase material) has a direct electronic band gap ~ 1.8 eV [1,2] while bulk 2H-phase MoS₂ exhibits a lower indirect band gap ~ 1.3 eV [3]. This semiconducting nature has been exploited to create MoS₂ field effect transistors (FETs) [4] with a high on-off ratio and ultrasensitive photodetectors [5], among other optoelectronic and photonic [6,7] devices. The number of layers not only provides tunability of the band gap of MoS₂ for photonic applications [8], but also performance enhancements that may not be directly gap related. For instance, the gas sensing behavior of few-layer thick MoS₂ has been found to be better than that of single-layer MoS₂ due to the instability of the single-layer form in reactive gas environments [9,10]. Another example is that few-layer MoS₂ usually displays a higher carrier mobility than that of single-layer MoS₂ in various heterostructured FET configurations [11–13].

The stacking sequence is a major structural factor that controls the properties of few-layer MoS₂. Theoretical calculations have predicted that the stacking sequence in bilayer MoS₂ plays an important role in its electronic band structure [14]. Experimental studies have found that the relative rotation angle in bilayer MoS₂ significantly modifies the direct/indirect band gap and interlayer coupling [15,16]. The recently observed spin/valley polarization in symmetry-breaking 3R-phase bulk MoS₂ (another commonly observed phase of bulk MoS₂) further elucidates the key role of stacking sequences (or crystal structure) in the properties of layered MoS₂ [17].

Single- and few-layer MoS₂ grown by chemical vapor deposition (CVD) methods have great potential in building next-generation electronics due to the inherent controllability and scalability [18,19] of CVD growth. A thorough understanding of the structure of CVD-grown MoS₂ is essential for a full exploration of its applications. Here, we demonstrate a precise determination of different stacking sequences in CVD-grown few-layer MoS₂ by employing atomic-resolution annular-dark-field (ADF) imaging in scanning transmission electron microscopy (STEM) using an unusually low electron beam energy (50 keV). Notably, this energy is much lower than the 80 keV threshold for knock-on damage to MoS₂ [20]; this allows for an extended study of pristine multilayer MoS₂ at the atomic scale. We find that the stacking sequence in CVD-grown MoS₂ is layer dependent, and can be a mixture of 2H and 3R phases of MoS₂ in trilayer form. Density functional theory (DFT) calculations confirm that the stacking sequences observed in our CVD-grown few-layer MoS₂ are among the most stable configurations.

II. EXPERIMENTAL AND THEORETICAL DETAILS

We use a two-zone furnace to grow single- and few-layer (bilayer and trilayer) MoS₂ on SiO₂/Si substrates, as described previously [21]. A quartz tube contains S and MoO₃ precursors, with S in zone 1 and MoO₃ precursor in zone 2. SiO₂/Si chips are placed on top of the crucible that contains the MoO₃ precursor. N₂ gas flows through the quartz tube during the whole growth process. Zones 1 and 2 are first kept at 105 °C for 3 h to warm up the precursors and 200 sccm N₂ flows through the tube. The temperature of zone 2 is then slowly increased to 500 °C (over 30 min) while zone 1 is kept at 105 °C. These temperatures are maintained for 30 min. The temperatures of zones 1 and 2 are then raised to 400 and 780 °C

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(over 30 min), respectively, and N_2 flow rate is changed to 9 sccm. The 400 and 780 °C temperatures are maintained for 10 min, after which the furnace is turned off and cooled to room temperature naturally.

We use optical microscopy and Raman spectroscopy to initially characterize single- and few-layer MoS_2 grown on SiO_2/Si by the CVD method (see examples shown in Supplemental Material Sec. 1 [22]) before transferring the flakes onto Quantifoil® TEM grids. Previous studies have shown that single-layer MoS_2 grown on SiO_2/Si by the CVD method displays a direct band gap and shows a strong photoluminescence (PL) peak centered around 1.84 eV at room temperature [18,19]. Double-layer CVD-grown MoS_2 has an indirect band gap and shows a slightly redshifted PL peak compared to the single-layer form. These distinctions aid in initial sample layer number identification.

TEM samples for STEM ADF imaging are prepared by a “direct transfer” [23]. A Quantifoil® TEM grid is placed on the targeted MoS_2 flakes grown on the SiO_2/Si substrate and a drop of isopropyl alcohol (IPA) is placed next to the TEM grid. After the IPA evaporates completely, the SiO_2/Si substrate with the TEM grid is placed into a potassium hydroxide (KOH) solution (~10%) overnight. After etching away the SiO_2 , the TEM grid with MoS_2 flakes is detached from the Si substrate. The TEM grid is then rinsed in de-ionized (DI) water several times. Immediately before imaging, the TEM grid with MoS_2 flakes is annealed in forming gas ($Ar : H_2 = 200$ sccm:50 sccm) at 250 °C for 3 h.

Atomic-resolution STEM ADF imaging is performed on TEAM 0.5, a double-aberration-corrected (scanning) transmission electron microscope (STEM/TEM) located in the National Center for Electron Microscopy (NCEM) at the Molecular Foundry, Lawrence Berkeley National Laboratory. The microscope is here operated at 50 keV to minimize radiation damage to the sample. For STEM ADF imaging, a probe size of ~ 1.7 Å, a convergence angle of 32 mrad, and collection angles of 77–385 mrad are used.

Total energy calculations are carried out using density functional theory (DFT) and the projector augmented-wave

(PAW) approach as implemented in the Vienna *ab initio* simulation package (VASP) [14,24,25]. The generalized gradient approximation (GGA) of Perdew-Burke-Ernzerhof (PBE) is used to approximate the electronic exchange and correlation. The interlayer van der Waals interactions are considered using a correction scheme by Grimme [26]. We model MoS_2 stacking using a slab model with a vacuum layer of at least 20 Å. All structures are relaxed until the energy has converged to within 10^{-6} eV/unit cell.

III. RESULTS AND DISCUSSION

As a member of transition metal dichalcogenides (TMDs) having rich polytypism [27], bulk MoS_2 presents two commonly observed phases: (1) the $2H$ phase (space group $P6_3/mmc$) which exists naturally and can also be synthesized via chemical vapor transport (CVT) methods, and (2) the $3R$ phase (space group $R3m$) which is typically synthesized (again via CVT methods) [17]. The stacking orders for both $2H$ and $3R$ phases, in the single-layer, bilayer, and trilayer configurations, are shown in Fig. 1. The nomenclature for the stacking sequence used here follows Refs. [14,28]. Single-layer MoS_2 for both phases has the same structure, with one layer of Mo atoms sandwiched between two layers of S atoms. Each layer of Mo and S atoms is arranged in a hexagonal lattice and two S layers have the same in-plane lattice points. For bilayer MoS_2 , the $2H$ and $3R$ phases show different stacking sequences for the S-Mo-S sandwiched structure. As shown in Fig. 1, $2H$ -phase MoS_2 in the form of a bilayer has a stacking sequence recorded as AA' , with Mo eclipsed over S, and the two layers have inversion symmetry. $3R$ -phase MoS_2 in the form of a bilayer has a stacking sequence AB , with staggered Mo over S, and the two layers do not have inversion symmetry. To determine the stacking sequence for trilayer MoS_2 of different phases, we treat the second layer as the first layer (as if it were A) and name the stacking sequence for the third layer following the two-layer naming system. Therefore, $2H$ -phase trilayer MoS_2 has a stacking sequence $(AA')A'$ and $3R$ -phase trilayer MoS_2 has the sequence $(AB)B$.

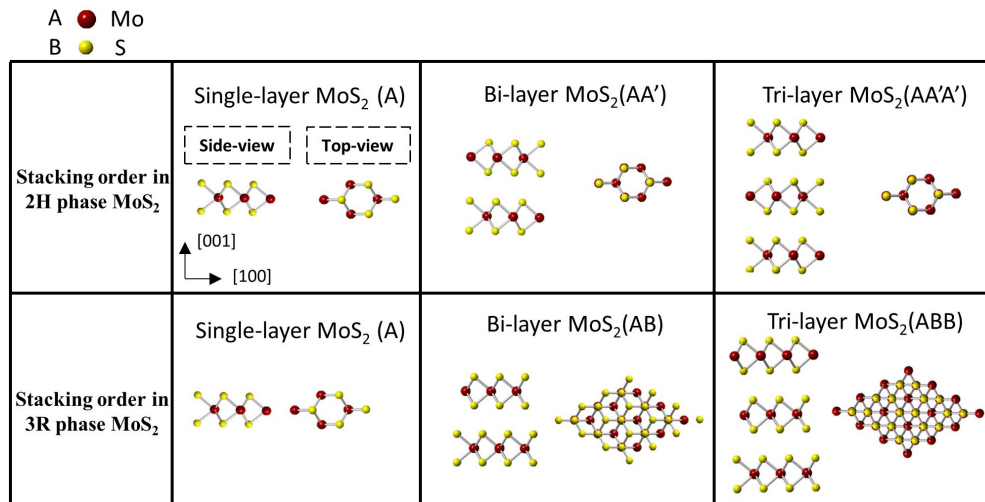


FIG. 1. Schematics showing the stacking orders for $2H$ and $3R$ phases MoS_2 in the single-layer, bilayer and trilayer forms viewed from side and top. Red spheres represent Mo atoms and yellow spheres represent S atoms.

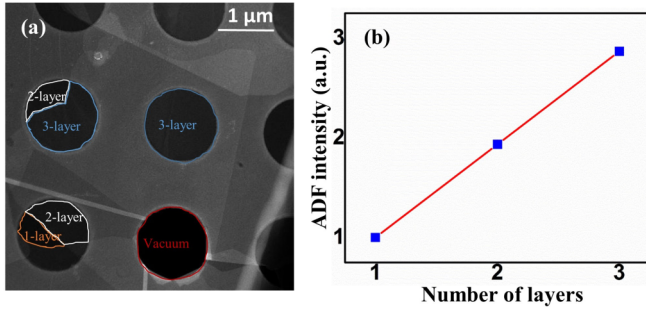


FIG. 2. Low-magnification ADF image of single-layer, bilayer, and trilayer MoS₂. (a) Low-magnification ADF image of the area where one-, two-, and three-layer CVD-grown MoS₂ hang over holes on a Quantifoil[®] TEM grid. The region of vacuum gives the background counts for the whole image. (b) The intensity in the ADF image is linear as a function of the number of layers after background subtraction using vacuum as reference.

ADF STEM imaging is a powerful tool to distinguish different atoms provided that the sample has uniform thickness [29]. Given that (1) MoS₂ is composed of two atomic species (Mo and S) which have significantly different atomic numbers (Mo 42, S 16), and (2) multilayer MoS₂ is a layered structure with uniform sample thickness for a certain number of layers, ADF imaging serves ideally to identify the type and location of each atom in thin samples. Figure 2 shows the low-magnification ADF image of single-layer, bilayer, and trilayer MoS₂ suspended over holes of the TEM grid. The layer number can be identified according to the linearly changed intensity in the image after background subtraction (using vacuum as a reference) as shown in Fig. 2(b).

With comparison to simulated ADF images of MoS₂ with known stacking sequences, we identify the stacking sequence in experimental ADF images of CVD-grown few-layer MoS₂. In order to improve the signal-to-noise ratio in the experimentally obtained ADF images, a few or tens of unit cells from a larger sample area are averaged [30] and presented in Figs. 3(a)–3(c), corresponding to single-layer, bilayer, and trilayer MoS₂, respectively [the same region as shown in Fig. 2(a)]. The original ADF images from larger areas of different layer numbers can be found in the Supplemental Material Sec. 2 [22]. Figures 3(d)–3(f) are simulated ADF images based on multislice theory [30]. These simulated images provide information regarding symmetry and relative intensity at different atomic sites for a certain stacking sequence. A match in terms of both symmetry and intensity between simulated and experimental ADF images is essential for the determination of the correct stacking sequence. Experimental ADF images are less sharp than the simulated ones due to incoherence and a broadening effect in the real-life electron probe, as well as drifting effects and sample vibration during the imaging process. In the experimental ADF images, one often finds overlapping of intensity between neighboring atoms, which blurs the atomic edges. The experimental ADF image of single-layer MoS₂ [Fig. 3(a)] shows distinct intensity at two sublattices for Mo and S, respectively, with red spheres representing Mo and overlapping yellow spheres representing S. A simulated ADF image of single-layer MoS₂ [Fig. 3(d)] shows the same

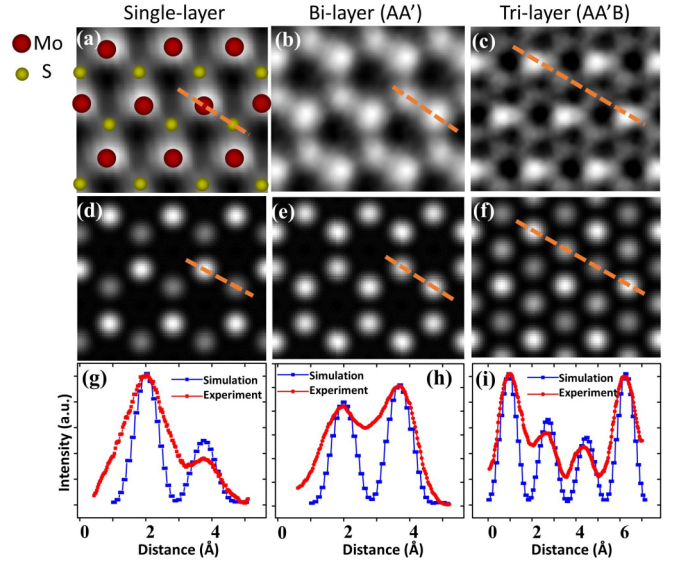


FIG. 3. Atomic-resolution ADF images of single-layer, bilayer (AA' stacking), and trilayer (AA'B stacking) CVD-grown MoS₂ in comparison with simulated images. (a)–(c) Experimentally observed atomic-resolution ADF images of single-layer, bilayer (AA' stacking), and trilayer (AA'B stacking) CVD-grown MoS₂, respectively, after averaging the intensity of more than 10 unit cells from a larger area of the same stacking sequence. (d)–(f) Multislice simulation of ADF images of single-layer, bilayer (AA' stacking), and trilayer (AA'B stacking) MoS₂ with the same beam energy, convergence angle, and collection angles for the experiment. (g)–(i) Line scans across lattice points indicated by the orange lines in (a)–(c) and (d)–(f), showing the comparison of intensity of these lattice points in simulated and experimental ADF images for single-layer, bilayer (AA' stacking), and trilayer (AA'B stacking) CVD-grown MoS₂, respectively.

symmetry as the experimental ADF image. The line scans across the Mo and S sublattice points in experimental and simulated images [Fig. 3(g)] show the same ratio of relative intensity. With the same analysis method, we find that a great portion (>50%) of bilayer CVD-grown MoS₂ takes the stacking sequence of AA'. An experimental ADF image of such a stacking sequence is shown in Fig. 3(b), in which we consistently observe intensity differences around 15% at two sublattices with threefold symmetry. This is in accord with the multislice simulation shown in Fig. 3(e). The line scans across the inequivalent two lattice points in experimental and simulated ADF images are compared in Fig. 3(h), which show a good match in relative intensity. Nonzero relative rotation angles between the two layers are also observed in our bilayer MoS₂ samples, which are common in CVD-grown MoS₂ (see Supplemental Material Sec. 3 [22] and Ref. [18]).

A new symmetry-breaking stacking sequence is found in our CVD-grown trilayer MoS₂. This stacking sequence is identified to be (AA')B after we compare the experimental and simulated ADF images of trilayer MoS₂ with stacking sequences that have AA' stacking for the first two layers (see Supplemental Material Sec. 4). In AA'B stacked trilayer MoS₂, the third layer is staggered, with S atoms over Mo atoms of the second layer, as shown schematically in Fig. 4(a). There are three distinct lattice points in AA'B stacked trilayer

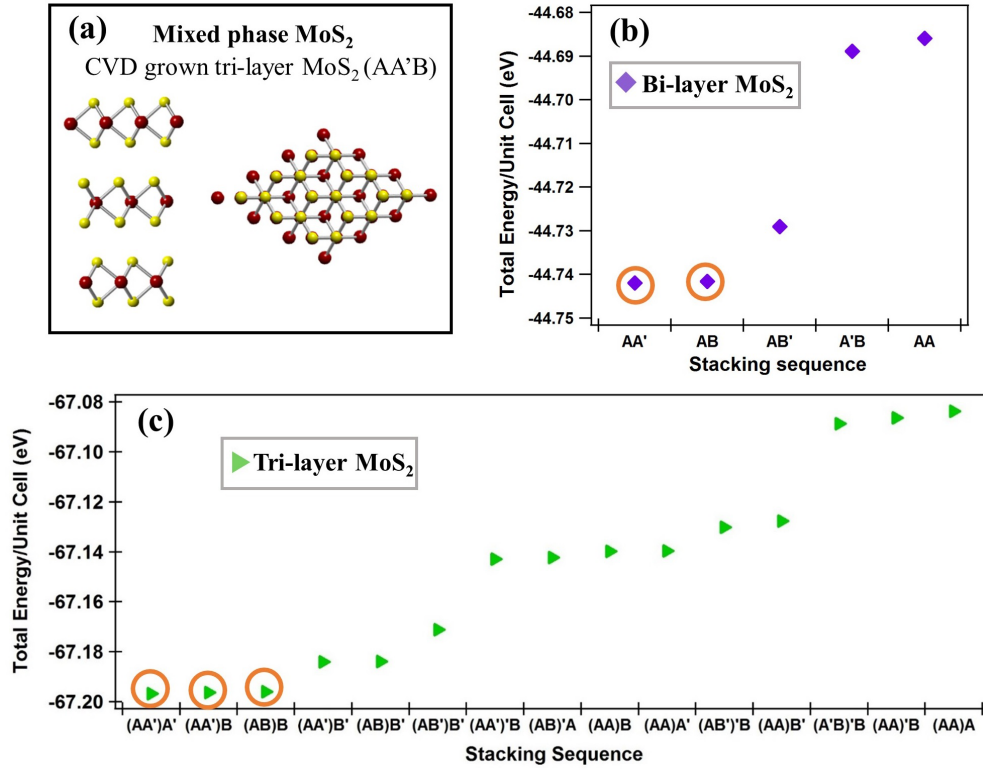


FIG. 4. (a) Crystal structure of trilayer MoS₂ with the stacking sequence AA'B viewed from the side (on the left) and top (on the right); (b) total energies of all possible stacking sequences for bilayer MoS₂, obtained from first-principles calculations; (c) total energies of all possible stable stacking sequences for trilayer MoS₂, obtained from first-principles calculations. Data points outlined by orange circles in (b) and (c) correspond to the stacking sequences with the lowest energies in bilayer and trilayer MoS₂, respectively.

MoS₂, as shown in the experimental [Fig. 3(c)] and simulated [Fig. 3(f)] ADF images. The line scans across these three lattice points [Fig. 3(i)] in experimental and simulated ADF images show that the ratio of intensity for these three lattice points is 1:0.55:0.45 and 1:0.65:0.5, respectively, in reasonable agreement. CVD-grown trilayer MoS₂ with a stacking sequence AA'B is consistently observed (>50%) across the same sample and in samples from different growth batches (see Supplemental Material Sec. 5 [22]).

To understand the prevalence of the AA'B stacking sequence over other stacking possibilities in the trilayer MoS₂, we perform first-principles calculations to study the preference of different stacking sequences of MoS₂. All possible bilayer (five) and trilayer (15) stacking sequences of MoS₂ are calculated and the total energies are compared in Figs. 4(b) and 4(c), respectively (absolute values for all stacking possibilities are in Supplemental Material Sec. 6 [22]). Here, the calculated energy is the total energy from solving the Kohn-Sham equation [31] plus the dispersion corrections by Grimme [26]. For bilayer MoS₂, as expected, the stacking sequences with the lowest energies are AA' and AB, which correspond to bilayer forms of the 2H and 3R phases, respectively [outlined by orange circles in Fig. 4(b)]. Our calculation results of bilayer MoS₂ are comparable to those of Ref. [14]. These two stacking sequences are close in energy and are commonly observed in experimental studies. In our CVD-grown bilayer MoS₂, AA' stacking is prevalent over AB stacking. Similarly, there are three trilayer stacking possibilities with nearly degenerate calculated energy, as

outlined by orange circles in Fig. 4(c): (AA')A', (AA')B, and (AB)B (the energy differences are within typical DFT error, so a true ground state is not determined). Importantly, the experimentally observed (AA')B stacking in CVD-grown trilayer MoS₂ is among these predicted minimum energy configurations. Moreover, the (AA')B stacking sequence is dominant in our CVD-grown trilayer MoS₂, and indicates that our growth conditions favor this stacking over other low-energy stacking sequences, probably due to the higher-energy barriers required by those stacking configurations.

CVD-grown few-layer MoS₂ with different stacking sequences reported here is relevant to the electronic and optical properties of this material. Specifically, distinct layer-dependent valley polarization phenomena in few-layer 2H and 3R phases of MoS₂ [17] suggest that trilayer CVD-grown MoS₂ with mixed stacking sequences (AA'B) may present a new valley polarization signature that is different from those of both phases of trilayer form. In addition, we speculate the layer-dependent stacking sequence observed in our CVD-grown few-layer MoS₂ is likely controlled synergistically by various growth parameters. These parameters include growth temperature, feeding rate, and partial pressure of the precursors, which can change slightly over time during the material's nucleation and growth process. Because CVD growth of few-layer MoS₂ follows the so-called "layer-by-layer" growth mechanism [32], the slight change in growth parameters over time will cause a change in the preferred stacking sequence for a certain layer number.

IV. SUMMARY AND CONCLUSIONS

Atomic-resolution STEM imaging is successfully employed to precisely determine different stacking sequences in few-layer CVD-grown MoS₂. The stacking sequences in bilayer and trilayer MoS₂ are found to differ. The 2H phase is consistently observed for bilayer CVD-grown MoS₂, which has the stacking sequence AA' with inversion symmetry. The stacking sequence AA'B is observed for the majority of CVD-grown trilayer MoS₂, which shows broken inversion symmetry. First-principles calculations show that the AA'B stacking sequence is among the most stable configurations, with the other two stacking possibilities of AA'A' (2H phase) and ABB (3R phase). Due to the symmetry-breaking nature of trilayer CVD-grown MoS₂, this configuration should be of great interest for valley polarization studies.

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