

Structural, magnetic, and optical properties of BiFeO₃ and Bi₂FeMnO₆ epitaxial thin films: An experimental and first-principles study

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BiFeO₃ and Bi₂FeMnO₆ films were epitaxially grown on SrTiO₃ (001) substrates by pulsed-laser deposition, and their structural, magnetic, magneto-optical and optical properties were measured. In Bi₂FeMnO₆, Fe is mainly present in the 3+ valence state, while Mn shows multivalence states. Bi₂FeMnO₆ exhibits low magnetization at room temperature and at 5 K indicating there is no significant *B*-site ordering. The BiFeO₃ film shows high optical transparency, while Bi₂FeMnO₆ shows high absorption loss in the infrared. Density-functional theory modeling of BiFeO₃, BiMnO₃ and Bi₂FeMnO₆ was carried out by applying the generalized gradient approximation (GGA) and GGA+*U* methods. The formation enthalpy of ordered Bi₂FeMnO₆ is positive for several crystal symmetries and for ferromagnetic (FM) or antiferromagnetic (AFM) spin structures at 0 K temperature, indicating *B*-site ordering is not favored. The electronic structure calculations are consistent with the electronic and optical properties of these films.

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I. INTRODUCTION

Ordered double perovskites, in which two different *B*-site cations form a superlattice within the ABO₃ perovskite structure, have attracted great interest recently.¹⁻⁵ Materials with such a structure may possess both ferromagnetic and ferroelectric, or ferromagnetic and ferroelastic properties, and are therefore multiferroics.⁶⁻⁸ Among these materials, room temperature (RT) ordered double perovskites with bismuth on the *A* site are particularly interesting. Due to the large orbital radius of the Bi 6s² lone pairs, the crystal structure of bismuth-based perovskites is usually distorted to low symmetries, producing large spontaneous ferroelectric polarization along certain crystallographic directions.⁹ At the same time, *B*-site ordering of transition-metal ions may make such materials ferromagnetic or ferrimagnetic. If the magnetic and ferroelectric properties couple with each other, these materials are intrinsic magnetoelectric multiferroics. Integrated magneto-optical isolators could provide another application for Bi-based ordered double perovskites.^{10,11} A magneto-optical isolator makes use of Faraday rotation to control the polarization direction of incident light. Due to their good lattice match with silicon, perovskite materials, especially orthoferrites (AFeO₃), might be suitable candidates for integrated isolators.¹² In order to obtain high Faraday rotation in perovskites, one has to line up most of the orbital angular momentum vectors of the active ionic electric dipoles along a macroscopic direction. This is usually achieved by spin-orbit coupling in a ferromagnetic or ferrimagnetic material. In other words, efficient Faraday rotators are usually ferromagnetic or ferrimagnetic at RT. In ordered double perovskites with Curie temperature (*T_C*) above RT, the spins and orbital angular momentum vectors of the two types of GGA+*U*-site ions align along their own macroscopic directions when magnetized, providing a net Faraday rotation at certain wavelengths.¹² Meanwhile, Bi³⁺ ions have strong covalent interactions with the octahedral complexes, which enhance the nondegeneracy of the spin-orbit coupling levels as

well as the Faraday rotation of the material.^{13,14}

Among the bismuth perovskites, perhaps BiFeO₃ is the most systematically studied.¹⁵⁻¹⁷ The Bi₂FeMnO₆ bulk crystal belongs to the *R3c* space group. The unit cell of BiFeO₃ can be considered to be a deformed ideal cubic perovskite. By moving Bi and Fe atoms along the pseudocubic [111] direction and O atoms along the pseudocubic ⟨110⟩ directions, the unit cell is elongated with the neighboring octahedrons rotated in different directions about the [111] axis.¹⁸ BiFeO₃ is antiferromagnetic with a Néel temperature of *T_N* ~ 640 K.^{19,20} The Fe spins form a *G*-type antiferromagnetic (*G*-AFM) structure, in which the spins are coupled ferromagnetically in the pseudocubic (111) planes and antiferromagnetically between neighboring (111) planes, so that each Fe atom couples antiferromagnetically with its nearest Fe neighbors.²¹ Besides BiFeO₃, another bismuth perovskite, BiMnO₃, is also well studied because of its multiferroic properties at low temperature.²² Due to the Bi 6s² lone pairs, the unit cell of the BiMnO₃ bulk crystal is distorted to *C2* symmetry at and below room temperature.²³ In contrast to BiFeO₃, BiMnO₃ is ferromagnetic with *T_C* ~ 105 K.²⁴ This is because ferromagnetic rather than antiferromagnetic superexchange between the *e_g* orbitals of neighboring Mn³⁺ ions is favored in the distorted unit cell.²⁵⁻²⁷ There are also several experimental studies on BiFe_{1-x}Mn_xO₃ bulk crystals and thin films.²⁸⁻³¹ A general finding is that incorporation of Fe in the Mn-rich side drives the material from ferromagnetic to antiferromagnetic, while adding Mn in the Fe-rich side results in higher saturation magnetization at room temperature.

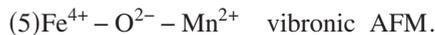
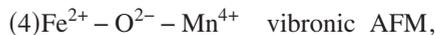
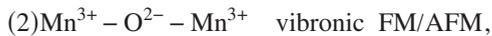
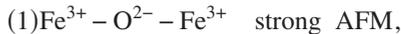
Despite these previous studies, there are several questions remaining. First, is *B*-site ordering likely to occur in certain double perovskite systems (specifically BiFe_{1-x}Mn_xO₃ in this study)? Previous experimental results indeed show that incorporating Mn into the BiFeO₃ lattice enhanced the magnetization,^{30,31} but whether this is caused by local *B*-site ordering is unclear. Second, for magneto-optical isolator applications, how do the Bi and *B*-site ions influence the optical and magneto-optical properties of these perovskites? Al-

though YFeO_3 and rare-earth-based orthoferrites show high optical transparency ($\alpha < 0.5 \text{ cm}^{-1}$) and high Faraday rotation constant at 1550 nm wavelength,^{32,33} as far as we know, the infrared optical and magneto-optical properties of bismuth perovskites and bismuth double perovskites have not been reported. In order to answer these questions, we first examine the spin ordering influences due to local magnetic exchange interactions among the various possible cation combinations. We then employ both experimental and first-principles calculation methods to investigate the structural, magnetic, and optical properties of BiFeO_3 and $\text{Bi}_2\text{FeMnO}_6$ epitaxial thin films.

II. SPIN ORDERING CONSIDERATIONS

Based on anticipated effects of local interactions in a generic ABO_3 perovskite lattice, the magnetic moment and Faraday rotation should be dominated by antiferromagnetic spin ordering. In a stoichiometric specimen of B or $\text{Bi}_2\text{FeMnO}_6$, the most stable valence for either Fe or Mn is 3+. For $\text{Fe}^{3+}(3d^5)$, the five spins are aligned in a half-filled $3d$ shell ($t_{2g}^3 e_g^2$) high-spin configuration as dictated by Hund's rule; for the same reason, $\text{Mn}^{3+}(3d^4)$ is in a high-spin $t_{2g}^3 e_g^1$ arrangement in octahedral B sites that is further stabilized by a strong Jahn-Teller axial distortion along the z axis.

An important characteristic of the perovskite lattice is the 180-degree cation-anion-cation bonds that involve the e_g orbitals in bonding/antibonding linkages with the oxygen $2p$ orbitals, while relegating the t_{2g} orbitals to nonbonding roles. According to the Goodenough-Kanamori rules for 180-degree superexchange couplings,²⁵ the expectations for five possible combinations in these compounds are

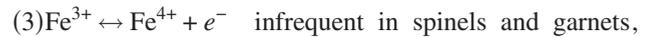
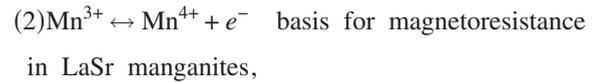


In case (1), both e_g orbitals are half-filled on both sides and present the classic case of correlated antiferromagnetism by virtual charge transfer. Case (2) is less certain because only one BiFeO_3 orbital is occupied, thereby producing a weaker AFM. However, if local Jahn-Teller effects become correlated, the AFM ordering can be overcome by a vibronic ferromagnetic (FM) ordering.²⁵⁻²⁷ In case (3) for dissimilar cations, a vibronic mechanism is also available, and the most likely result would be a moderate-to-weak antiparallel spin stabilization that is partially offset by delocalization FM exchange between a half-filled and empty pair of overlapping e_g orbital states.

If Fe and Mn are spatially ordered in the B sites, despite an antiparallel alignment a quasi-ferrimagnetic effect could be observed as a net one Bohr magneton moment from the difference between the opposing Fe^{3+} ($S=5/2$) and Mn^{3+}

($S=2$) moments. Cases (4) and (5) are less likely ionic states based on ionization potentials and Madelung energy considerations. The meager Faraday rotation data also indicate that $\text{Fe}^{3+}/\text{Mn}^{3+}$ ferrimagnetic ordering is not likely since some kind of interionic charge transfer would be necessary to satisfy the $\Delta S=0$ selection rule for allowed electric dipole transitions.^{12,34}

If the specimen is nonstoichiometric, polaronic conduction between mixed-valence cations (double exchange) can create FM properties by any of the following mechanisms (listed according to frequency of occurrence), with effectiveness determined by the particular bonding stabilization and activation energy:



Charges can transport by tunneling at low temperatures or by thermal activation (random hopping) when T approaches the Debye temperature. Note also that static as well as dynamic magnetoelastic effects from Fe^{2+} , Mn^{3+} , or $C2$ can be expected in each situation.

III. EXPERIMENTAL METHODS

BiFeO_3 and $\text{Bi}_2\text{FeMnO}_6$ thin films were fabricated using pulsed-laser deposition (PLD) with a Coherent COMPexPro 205 KrF (248 nm) excimer laser. The pulse frequency was 10 Hz and the fluence was about 2.5 J/cm^2 . $\text{Bi}_{1.2}\text{FeO}_3$ and $\text{Bi}_{2.4}\text{FeMnO}_6$ ceramic targets were fabricated by conventional solid-state reaction methods. Before deposition, the chamber was pumped to a vacuum level of 1×10^{-6} torr. By flowing pure O_2 , the oxygen partial pressure P_{O_2} was controlled at various levels from 2×10^{-7} torr to 15 mTorr during deposition. MgO and SrTiO_3 (STO) single crystals with (001) orientations were used as substrates. During deposition, the substrates were held at various temperatures (T_s) ranging from 530 to 680 °C.

Phase identification was performed using both conventional one-dimensional x-ray diffraction (1DXRD, Rigaku RU300) and two-dimensional x-ray diffraction methods [2DXRD, Bruker D8 with General Area Detector Diffraction System (GADDS)].³⁵ Element depth profiles of both materials were characterized using a Physical Electronics Model 660 scanning Auger microprobe. Depth profiling was performed using Ar^+ ion sputtering over a sample area of $3 \times 3 \text{ mm}^2$. The milling speed was 0.033 nm/s. B -site ion valence states of both films were identified on a Kratos AXIS Ultra imaging x-ray photoelectron spectrometer. The $\text{Bi } 4f_{7/2}$ peak with binding energy of 158.8 eV was used for energy calibration. Magnetic characterization was performed with vibrating sample magnetometry (VSM) using an ADE Technologies VSM Model 1660. The optical constants (the refrac-

TABLE I. Bi:Fe atomic ratios of BiFeO₃ films grown on MgO (001) substrates at various substrate temperatures and oxygen partial pressures.

	530 °C	580 °C	630 °C	680 °C
Vacuum		0.325	0.199	0.230
3 mTorr O ₂	0.648	0.850	0.800	0.382
7.5 mTorr O ₂	1.477	0.980	0.961	0.670
15 mTorr O ₂		1.338	1.307	

tive index n and extinction coefficient k) were characterized from 400 to 1700 nm wavelengths for both films on a WVASE32 ellipsometer. General oscillator models were applied to fit the optical constants, and the fitting root-mean-square error (MSE) was smaller than 1 for both materials. In order to check the validity of the modeling, we also measured transmission spectra for both samples on a Cary 500i UV-Vis-NIR dual-beam spectrophotometer with a range from 175 to 2000 nm. Magneto-optical characterization, i.e., the measurement of Faraday rotation angle as a function of applied magnetic field, was performed at 1550 nm on a custom-built apparatus described in Ref. 36. Composition measurements were performed by wavelength dispersive spectroscopy (WDS).

IV. EXPERIMENTAL RESULTS

A. Element stoichiometry and phase diagram

Table I shows the WDS results for BiFeO₃ films grown on MgO (001) substrates at various T_s and P_{O_2} . The bismuth versus iron atomic ratio shows a strong dependence on T_s and P_{O_2} during growth. Near-stoichiometric films can only be achieved in a small process window. Note that either high T_s or low P_{O_2} yield iron-rich films, while either low T_s or high P_{O_2} yield bismuth-rich films. The bismuth deficiency is due to the evaporation of bismuth at high T_s or low P_{O_2} , which is consistent with several previous reports,^{15,16,37} and which is partly offset by the use of Bi-rich targets.

The phase diagram of Bi₂FeMnO₆ as a function of P_{O_2} and T_s during growth is shown in Fig. 1, from data obtained by 2DXRD analysis. For comparison, the results on both STO and MgO substrates are shown. First we notice that

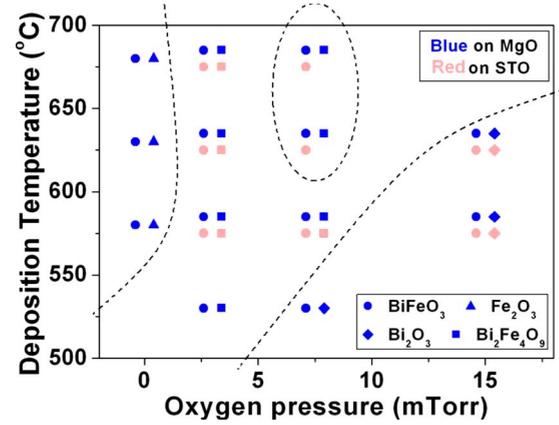


FIG. 1. (Color online) The phases forming during film growth in BiFeO₃ deposited on MgO (001) and SrTiO₃ (001) substrates as a function of substrate temperature and oxygen partial pressure. The dashed lines separate the conditions under which Fe₂O₃, Bi₂O₃ or BiFeO₃ perovskite phases dominate. The single-phase perovskite is formed at intermediate pressures and high temperatures on SrTiO₃ substrates.

either high T_s or low Bi₂FeMnO₆ favors the growth of γ -Fe₂O₃ (maghemite), while either low T_s or high P_{O_2} gives Bi-rich films and favors the growth of Bi₂O₃. Second, in most of the intermediate temperature and pressure range, BiFeO₃ and Mn₃O₄ coexist on both substrates. On MgO there is no process window for the growth of single-phase perovskite BiFeO₃, while on STO, there is a narrow window favoring single-phase BiFeO₃ growth, because the BiFeO₃ phase is stabilized by epitaxial growth on the STO substrate.³⁷ Considering the stoichiometry and phase diagram of BiFeO₃, it is clear that the atomic ratio of bismuth to iron determines the final phases in the film, and this compositional stoichiometry shows a stronger dependence on P_{O_2} than on T_s . Single phase BiFeO₃ films can only be obtained by pseudomorphic growth on a lattice-matched substrate at a P_{O_2} and T_s chosen to give correct film stoichiometry.

Table II shows the phase and compositional analysis of Bi₂FeMnO₆ films grown on STO substrates. In this system, we fixed T_s at 680 °C and varied P_{O_2} to obtain epitaxial growth of the perovskite phase. Two samples were annealed *in situ* in the PLD chamber for 2 h at the growth conditions before cooling down. The general trend of increasing Bi:(Fe+Mn) with P_{O_2} follows that seen in BiFeO₃, but *in*

TABLE II. Phases and compositions of Bi₂FeMnO₆ films grown on SrTiO₃ (001) substrates at 680 °C and various oxygen partial pressures. Two of the samples were *in situ* annealed at the pressure and temperature of the fabrication conditions for 2 h before characterization.

P_{O_2} (mTorr)	Phases	Bi/(Fe+Mn) (at. %)	Fe/Mn (at. %)
0.8	Bi ₂ FeMnO ₆ , γ -Fe ₂ O ₃ , Mn ₃ O ₄	0.94	0.91
1	Bi ₂ FeMnO ₆	1.07	0.92
3.5	Bi ₂ FeMnO ₆ , Bi ₂ O ₃	1.10	0.91
2.5 (<i>in situ</i> annealed)	Bi ₂ FeMnO ₆ , Bi ₂ O ₃ , γ -Fe ₂ O ₃ , Mn ₃ O ₄	0.56	0.95
7.5 (<i>in situ</i> annealed)	Bi ₂ FeMnO ₆ , Bi ₂ O ₃ , γ -Fe ₂ O ₃ , Mn ₃ O ₄	0.65	0.94

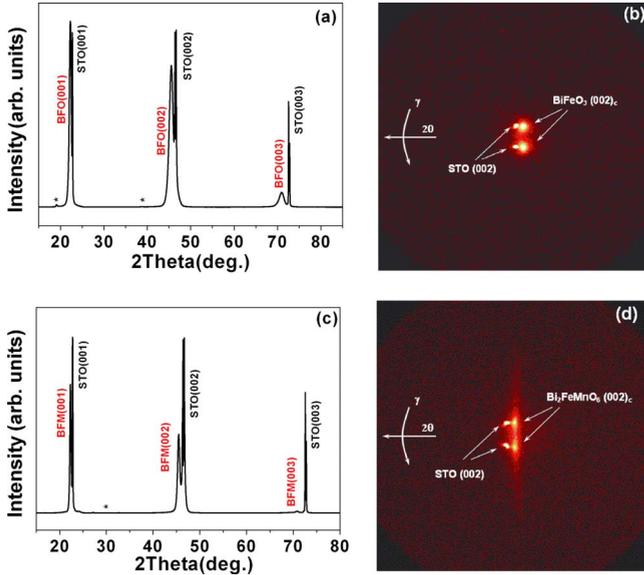


FIG. 2. (Color online) 1DXRD diffraction spectra for (a) BiFeO₃ and (c) Bi₂FeMnO₆ epitaxial films on SrTiO₃ (001) substrates. “*” indicates peaks from a trace amount of Bi₂O₃. Also shown are the 2DXRD pseudocubic (002)_c diffraction patterns of (b) BiFeO₃ and (d) Bi₂FeMnO₆ films. Both patterns were taken at an x-ray incident angle of $\theta=23^\circ$ and the frame center was $2\theta=46^\circ$. The data collection region is $31^\circ \leq 2\theta \leq 61^\circ$ and $75^\circ \leq \gamma \leq 105^\circ$. The samples were rotated by 360° about the axis normal to the sample surface during the measurement.

situ annealing leads to significant loss of Bi and formation of additional Fe and Mn oxides. A single-phase growth window is found around $P_{O_2}=1$ mTorr for unannealed samples. Compared with BiFeO₃ growth, Bi₂FeMnO₆ single-phase growth is more sensitive to fluctuations in fabrication conditions. For example an oxygen pressure change of ± 0.2 mTorr away from 1 mTorr will lead to formation of significant amounts of secondary phases, indicating that Bi₂FeMnO₆ is even less stable than BiFeO₃. The Fe:Mn atomic ratio is close to 1 and independent of oxygen pressure.

Based on these results, optimum conditions were chosen to grow epitaxial BiFeO₃ and Bi₂FeMnO₆ films with only trace amounts of impurity phases (mainly α -Bi₂O₃ or β -Bi₂O₃) on STO (001) substrates for further analysis. The thickness of the BiFeO₃ and Bi₂FeMnO₆ films was 850 and 220 nm, respectively, as confirmed by profilometer. The 1DXRD and 2DXRD spectra of both films are shown in Figs. 2(a)–2(d). Both BiFeO₃ and Bi₂FeMnO₆ show (00k)_c pseudocubic diffraction peaks in the 1DXRD spectrum, while the well-defined spotlike diffraction patterns on 2DXRD spectra indicate both films are epitaxially grown on STO. The 1DXRD spectra show that Bi₂FeMnO₆ has a larger out-of-plane lattice parameter than BiFeO₃. The in-plane lattice parameter analysis of the (122), (202) and (112) diffraction peaks of both films were carried out by 2DXRD. By fitting the lattice spacing, we obtained all the lattice parameters for both films. BiFeO₃ has a monoclinic unit cell with $a=b=4.037$ Å, $c=3.947$ Å, and $90^\circ-\beta=-0.88^\circ$, while Bi₂FeMnO₆ has a monoclinic unit cell with $a=3.915$ Å,

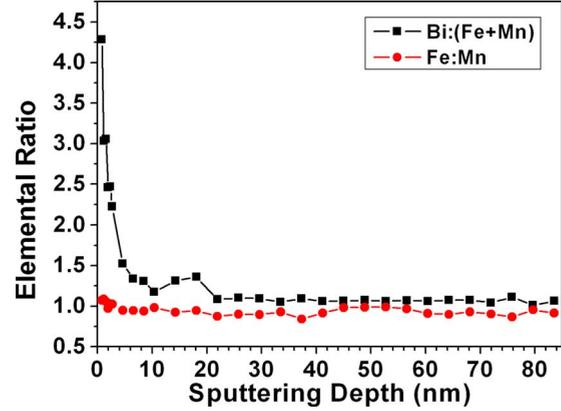


FIG. 3. (Color online) Bi:(Fe+Mn) and Fe:Mn atomic ratios in a Bi₂FeMnO₆ film as a function of depth, from Auger electron spectroscopy.

$b=3.935$ Å, $c=3.986$ Å and $90^\circ-\beta=-0.5^\circ$, where β is the angle between the a and b directions. Both films are distorted to monoclinic symmetry with c axis out-of-plane by their epitaxial relation with the substrate. Bi₂FeMnO₆ shows a smaller unit-cell volume (61.40 Å³) compared with BiFeO₃ (64.31 Å³). Compared with the SrTiO₃ substrate (cubic cell with $a=3.905$ Å and unit-cell volume 59.55 Å³), the largest in-plane lattice mismatch of BiFeO₃ and Bi₂FeMnO₆ are 3.4% and 0.8%, respectively. Although better lattice matching is achieved in Bi₂FeMnO₆, the film quality is not as good as for BiFeO₃. At a Bi₂FeMnO₆ thickness of 220 nm, a small amount of impurity phase is observed, and this increases with thickness. In contrast, for BiFeO₃, epitaxial film growth was achieved at a thickness of 850 nm, and the impurity phase was limited to a trace amount. This observation suggests that the perovskite phase of Bi₂FeMnO₆ is less stable compared with BiFeO₃.

B. Element depth profile and valence states

Auger electron spectroscopy (AES) was carried out to measure the element depth profile of both samples. Figure 3 shows the result on the Bi₂FeMnO₆ film. The Bi:(Fe+Mn) atomic ratio is 4.5 at the film surface but decreases to 1 within 10 nm film thickness, while the Fe:Mn atomic ratio remains almost constant. There is no change in either ratio for the remaining thickness of the film. This surface bismuth-rich layer is also found in the BiFeO₃ film according to AES and XPS surface analysis. However, due to large charging effects in this film, we could not obtain a clear AES depth profile spectrum. The bismuth-rich surface layer was found previously in epitaxial BiFeO₃ films and was attributed to strain relaxation along the thickness direction of the film.³⁷ This effect causes the BiFeO₃ phase to have a higher free energy of formation than Bi₂O₃ near the film surface, favoring the growth of the latter.

Figures 4(a)–4(c) show the XPS core level spectra of Fe 2p in BiFeO₃, and Fe 2p and Mn 2p in Bi₂FeMnO₆, respectively. To assure our analysis was carried out on the perovskite phase, Ar⁺ ion milling was performed until the bismuth concentration was stable in survey scans. The XPS

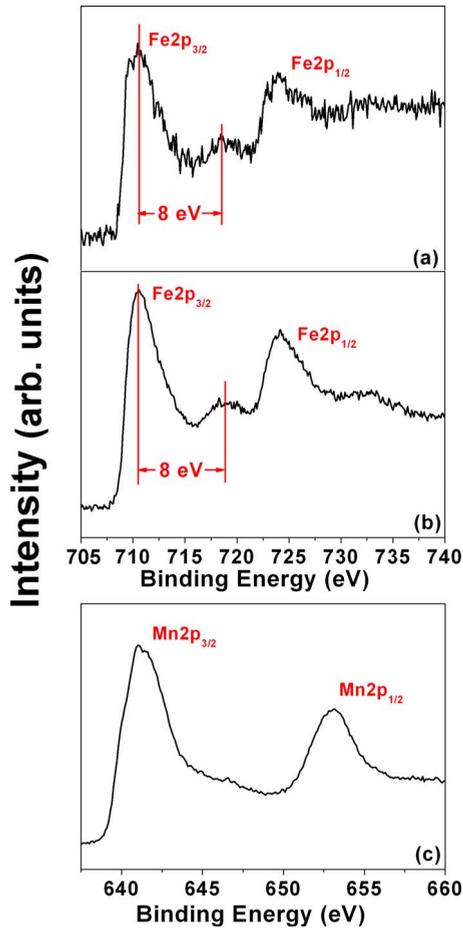


FIG. 4. (Color online) XPS spectra of the Fe $2p$ peaks for (a) BiFeO_3 and (b) $\text{Bi}_2\text{FeMnO}_6$ and (c) the Mn $2p$ peaks for $\text{Bi}_2\text{FeMnO}_6$.

spectra of Fe and Mn reveal the usual $2p_{3/2}$ and $2p_{1/2}$ doublet arising from spin-orbital interaction. Comparing both spectra we found that the Fe $2p$ lines resemble each other in BiFeO_3 and $\text{Bi}_2\text{FeMnO}_6$ films. The binding energy of the Fe $2p_{3/2}$ level is 710.57 eV in BiFeO_3 and 710.61 eV in $\text{Bi}_2\text{FeMnO}_6$. No shoulder peak was found around the Fe $2p_{3/2}$ peak in either sample. Moreover, a satellite peak was found about 8.0 eV above the Fe $2p_{3/2}$ principal peak. This satellite peak is considered to be characteristic of the oxidation state of the Fe.²⁹ Due to different d orbital electron configurations, during relaxation of the metal ions, Fe^{2+} and Fe^{3+} will show a satellite peak at 6 eV or 8 eV above their $2p_{3/2}$ principal peaks, respectively.³⁸ The structure and similarity of the Fe $2p$ core level spectra in both BiFeO_3 and $\text{Bi}_2\text{FeMnO}_6$ films indicate that Fe is mainly in the $3+$ valence state in both systems. On the other hand, in the $\text{Bi}_2\text{FeMnO}_6$ film, the Mn $2p_{3/2}$ principal peak has a binding energy of 642.2 eV. A shoulder peak below this energy originates from Mn^{2+} and indicates the presence of multiple valence states of Mn. In the stoichiometric $\text{Bi}_2\text{FeMnO}_6$, the average valence state of the B -site cation is $3+$, and since Fe is mainly present as $3.75 \mu_B$, this suggests that Mn must exhibit Mn^{2+} , Mn^{3+} , and Mn^{4+} valence states. Previous XPS analysis on 10 at. % Mn-doped BiFeO_3 indicates that the oxidation state of Fe

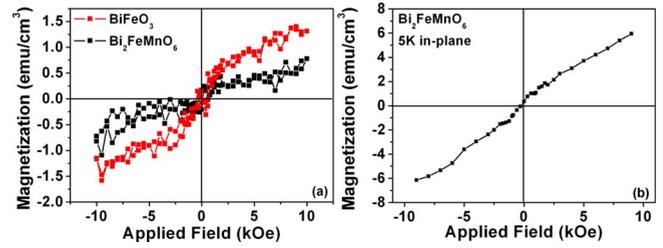


FIG. 5. (Color online) (a) Magnetization as a function of out-of-plane applied field for BiFeO_3 and $\text{Bi}_2\text{FeMnO}_6$ films at room temperature. (b) In-plane magnetization of a $\text{Bi}_2\text{FeMnO}_6$ film measured by SQUID magnetometry at 5 K. The plot shows a half loop scanning from -9000 to 9000 Oe.

was primarily $3+$.²⁹ From our analysis this effect seems to persist even with 50 at. % Mn present in the B sites.

C. Magnetic and magneto-optical properties

Figure 5(a) shows the out-of-plane magnetic hysteresis loops of BiFeO_3 and $\text{Bi}_2\text{FeMnO}_6$ films measured at room temperature by VSM. The data were obtained by subtracting the substrate magnetization from the overall hysteresis of the samples. Both samples show low and nonsaturating magnetization for an applied magnetic field up to 10 kOe. BiFeO_3 exhibits a magnetization of 1.2 emu/cm^3 at 1 kOe resulting from slight canting of the antiferromagnetically-coupled moments, while $\text{Bi}_2\text{FeMnO}_6$ exhibits an even smaller magnetization of 0.8 emu/cm^3 . These results suggest that the magnetization in $\text{Bi}_2\text{FeMnO}_6$ also originates from canted antiferromagnetism at room temperature. In order to investigate the magnetic ordering of $\text{Bi}_2\text{FeMnO}_6$ at low temperatures, we measured the magnetization of $\text{Bi}_2\text{FeMnO}_6$ at 5 K using a superconducting quantum interference device (SQUID) magnetometer, as shown in Fig. 5(b). $\text{Bi}_2\text{FeMnO}_6$ shows nonsaturating behavior at this temperature. The magnetization at 9 kOe is estimated at 5.4 emu/cm^3 , corresponding to $0.03 \mu_B$ per B -site ion. This value is far from the values expected if the Fe and Mn atoms were ordered in the B sites ($4 \mu_B$ for ferromagnetic or $0.5 \mu_B$ for antiferromagnetic ordering of Fe^{3+} and Mn^{3+}), which indicates most of the B -site cations are disordered in this sample.

Faraday rotation hysteresis loops of both films at a wavelength of 1550 nm at room temperature were also measured on both samples. Due to the very low magnetization of both samples, no clear hysteresis was obtained. By subtracting the Faraday rotation signal from our substrate, we estimated the Verdet constant (Faraday rotation per unit length, per unit field strength for light traveling along the applied magnetic field direction in a magneto-optical medium) for both films. BiFeO_3 shows a Verdet constant of $18 \pm 2^\circ/\text{cm kOe}$, while $\text{Bi}_2\text{FeMnO}_6$ shows a Verdet constant of $50 \pm 3^\circ/\text{cm kOe}$.

D. Optical properties

Figure 6(a) shows the fitted optical constants for the BiFeO_3 film as a function of wavelength. At 1550 nm wavelength, the refractive index is $n=2.592$ and k is smaller than the detection error of the equipment. The small extinction

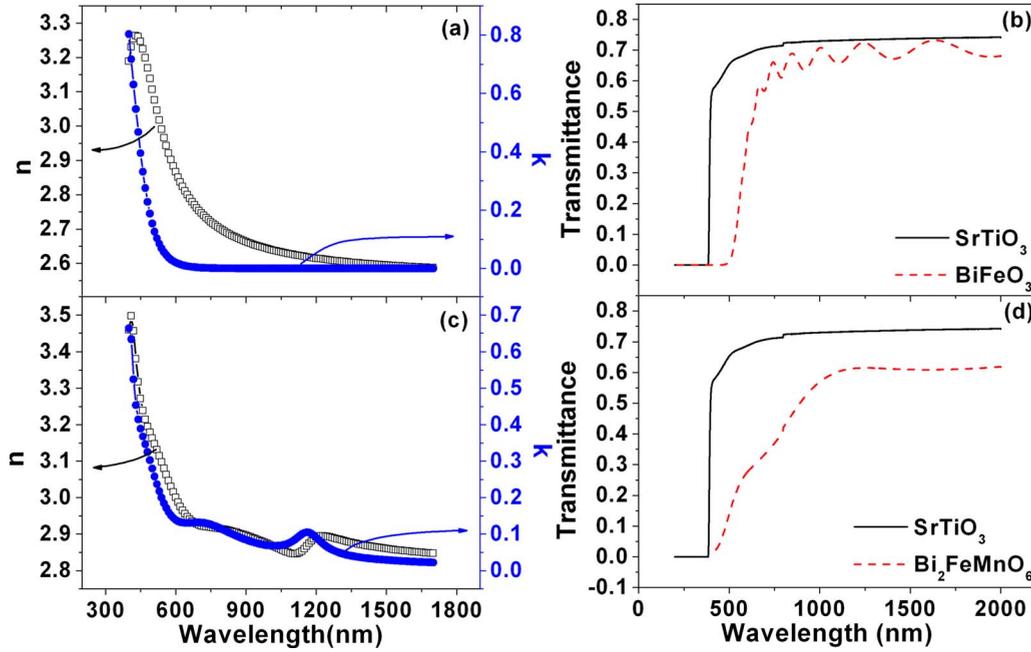


FIG. 6. (Color online) Optical constants as a function of wavelength for (a) BiFeO₃ and (c) Bi₂FeMnO₆ films as measured by ellipsometry; incident light transmittance as a function of wavelength for (b) BiFeO₃ and (d) Bi₂FeMnO₆ films as measured by spectrophotometry.

coefficient indicates BiFeO₃ is very transparent, similar to yttrium and other rare-earth orthoferrites in the infrared wavelength region.^{32,33} The validity of our fitting is supported by comparing the n , k data with the spectrophotometry absorption spectra shown in Fig. 6(b). First, the optical band gaps of BiFeO₃ measured by both methods are very similar. If one estimates the band gap of BiFeO₃ by the photon energies at the optical absorption edge, the measured band gap for BiFeO₃ is 2.44 eV by ellipsometry and 2.42 eV by spectrophotometry. Second, using the fitted film thickness, the n , k data and the substrate optical constants, we can obtain a good fit to the experimental absorption spectrum. Note that our fitting did not include the absorption peaks located around 1.0 and 0.7 μm caused by Fe³⁺ ${}^6A_1 \rightarrow {}^4T_1$ and ${}^6A_1 \rightarrow {}^4T_2$ crystal-field transitions, which will result in underestimation of the extinction coefficient around these wavelengths. But from both the results of ellipsometry and spectrophotometry, it is clear that BiFeO₃ has low optical absorption loss at 1550 nm wavelength.

Figure 6(c) shows the fitted optical constants for the Bi₂FeMnO₆ film as a function of wavelength. Quite different from BiFeO₃, this film shows a refractive index of $n=2.85$ and an extinction coefficient of $k=0.048$ at 1550 nm wavelength. We modeled both the surface layer and the underlying Bi₂FeMnO₆ film in this case, because the Bi-rich surface layer thickness is not negligible compared with the overall thickness of this sample. Also, an absorption peak is clear around 1100 nm wavelength. The high extinction coefficient of Bi₂FeMnO₆ film is confirmed by the spectrophotometer results shown in Fig. 6(d). The Bi₂FeMnO₆ sample has a much lower transmittance in the infrared region compared with the bare STO substrate.

V. FIRST-PRINCIPLES METHODS AND RESULTS

The difficulty in analyzing a multi-cation system wherein the distribution of magnetic ions is neither rigorously or-

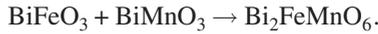
dered nor random (likely the case for Fe and Mn in Bi₂FeMnO₆) is compounded by the occurrence of variable valence states among the B -site cations. Regrettably, a semi-empirical “mean” field solution often becomes the best option. In this case, however, where there is no magnetic dilution of the B lattice, band theory computations might clarify the homogeneity question and serve as a bridge between the local expectations and a molecular field approach. In order to understand the structure, electronic structure, and magnetic properties of BiFeO₃ and Bi₂FeMnO₆, we therefore applied density-functional theory with spin polarized generalized gradient approximation (GGA) and GGA+ U (Liechtenstein’s implementation)³⁹ methods to calculate the structure and electronic structure of both materials. Projected augmented wave (PAW)⁴⁰ pseudopotentials are used, as implemented in the vienna *ab initio* simulation package (VASP).⁴¹ The cut-off energy was 500 eV. $5 \times 5 \times 5$, $3 \times 3 \times 3$ and $3 \times 3 \times 3$ k -point meshes were used for BiFeO₃, BiMnO₃ and Bi₂FeMnO₆, respectively. Full relaxation of the atomic coordinates and lattice vectors was achieved using both GGA and GGA+ U energy functionals until the total ground-state energies converged within 3 meV for each unit cell. The screened Coulomb interaction parameter U and exchange parameter J enter the Hamiltonian to account for the on-site electron-electron interactions in the localized $3d$ orbitals for Fe and Mn. In this work, we set $U=J=0$ eV for GGA calculations. For GGA+ U calculations, we fixed $J(\text{Fe})=J(\text{Mn})=1$ eV, and varied $U(\text{Fe})$ or $U(\text{Mn})$ from 4 to 8 eV.

We assumed the space group for BiFeO₃ and BiMnO₃ to be $R3c$ and $C2$, respectively, according to experimental results,^{15,22} while we varied the space groups for Bi₂FeMnO₆ unit cell to be $Pm\bar{3}m$, $R3$, and $C2$. The magnetic configurations for BiFeO₃ and BiMnO₃ were set to be G -AFM and FM, respectively. For Bi₂FeMnO₆, both FM and G -AFM configurations are presumed for each structural symmetry. In

TABLE III. Calculated lattice parameters of BiFeO₃ (space group $R3c$), BiMnO₃ (space group $C2$), and Bi₂FeMnO₆ (space groups $Pm\bar{3}m$, $R3$, and $C2$) calculated using the GGA+ U method. Also shown is the formation enthalpy of Bi₂FeMnO₆. G -AFM and FM magnetic ordering were assumed for BiFeO₃ and BiMnO₃, respectively. Both FM and G -AFM ordering were assumed for Bi₂FeMnO₆. $U(\text{Fe})=7$ eV, $J(\text{Fe})=1$ eV, $U(\text{Mn})=6$ eV, and $J(\text{Mn})=1$ eV were used for all calculations.

Space group	BiFeO ₃		BiMnO ₃		Bi ₂ FeMnO ₆		
	$R3c$	$C2$	$Pm\bar{3}m$		$R3$	$C2$	
Magnetic ordering	G -AFM	FM	FM	G -AFM	FM	FM	G -AFM
$a(\text{\AA})$	5.67	9.71	7.86	7.84	5.71	9.50	9.50
$b(\text{\AA})$	5.67	5.70	7.86	7.84	5.71	5.80	5.77
$c(\text{\AA})$	5.67	10.00	7.86	7.84	5.71	9.78	9.76
$\alpha(^{\circ})$	59.11	90	90	90	59.15	90	90
$\beta(^{\circ})$	59.11	111.11	90	90	59.15	107.91	107.91
$\gamma(^{\circ})$	59.11	90	90	90	59.15	90	90
$\Omega(\text{\AA}^3)$	126.28	516.33	485.83	482.04	129.09	512.74	508.91
Formation enthalpy per Bi basis (eV)	N/A	N/A	1.162	1.155	0.203	0.092	0.057

order to investigate how Mn valence state influences the unit-cell structure, we also varied Mn to be Mn²⁺, Mn³⁺, and Mn⁴⁺ by starting with different spin configurations on the Mn atoms. As a consequence, Fe was set to be Fe⁴⁺, Fe³⁺, Fe²⁺, respectively in these configurations. To estimate the formation enthalpy of Bi₂FeMnO₆, we considered the following reaction at 0 K temperature:



The formation enthalpy of Bi₂FeMnO₆ was estimated as

$$\Delta H_f = E(\text{Bi}_2\text{FeMnO}_6) - E(\text{BiFeO}_3) - E(\text{BiMnO}_3),$$

where E is the total energy after structure relaxation. By fixing BiFeO₃ and BiMnO₃ in the $R3c$ and $C2$ space groups, respectively, we can compare the formation enthalpy of Bi₂FeMnO₆ with different symmetries. Note that we neglect the small $P\Delta V$ term. This is applicable for reactions at atmosphere pressure, but it is not applicable for reactions carried out at high pressures such as several GPa.

A. Structure and formation enthalpy

Table III shows the structural parameters of BiFeO₃, BiMnO₃, and Bi₂FeMnO₆ and the formation enthalpy of Bi₂FeMnO₆ after unit-cell relaxation. We fixed $U(\text{Fe})=7$ eV and $U(\text{Mn})=6$ eV for all related calculations. The calculated BiFeO₃ and BiMnO₃ lattice parameters show good agreement with experimental data.^{42,43} For Bi₂FeMnO₆ there are three noticeable features in the calculation results. First of all, the formation enthalpy of Bi₂FeMnO₆ is always positive for all the structures and magnetic orderings we examined, suggesting that B -site ordered Bi₂FeMnO₆ is unstable at 0 K. The positive formation enthalpy comes from the Fe and Mn octahedrons as nearest neighbors. Thus, checkerboard-type B -site ordering is thermodynamically unfavored. Second, both the unit-cell structure and magnetic ordering affect the formation enthalpy of Bi₂FeMnO₆, with the former having the larger influence. The most stable struc-

ture of Bi₂FeMnO₆ is monoclinic with $C2$ space group. This result is not hard to interpret if one compares Bi₂FeMnO₆ with the lattice structure of BiMnO₃. In both systems Mn stays at the 3+ valence state, which creates a large lattice distortion due to the Jahn-Teller effect. This distortion is uniaxial, which distorts the unit cell from cubic to tetragonal. Meanwhile, the $6s^2$ lone pair states on Bi³⁺ ions further distort the unit cell to a noncentrosymmetric structure.⁹ Note that we cannot obtain stable antiferromagnetic spin ordering during lattice relaxation in Bi₂FeMnO₆ with $R3$ symmetry. Third, by comparing the formation enthalpy of Bi₂FeMnO₆ with FM and AFM magnetic ordering, one finds that AFM ordering is more stable for Bi₂FeMnO₆ with both $Pm\bar{3}m$ and $C2$ symmetries.

In order to verify the effect of cation valence state, we fixed the unit cell of Bi₂FeMnO₆ with $C2$ symmetry and varied the Mn valence states between Mn²⁺, Mn³⁺, and Mn⁴⁺. As a consequence, Fe is set as Fe⁴⁺, Fe³⁺, and Fe²⁺, respectively. Fe and Mn are antiferromagnetically coupled in these calculations. However, after lattice relaxation, all three cases relax to a Fe³⁺/Mn³⁺ configuration, indicating this configuration is thermodynamically most stable. This result is consistent with our XPS measurement that both Fe and Mn ions are mostly in the 3+ valence state. However, experimentally we observed small amount of Mn²⁺ and Mn⁴⁺ in our films. One possible explanation may be related to the behavior of Mn³⁺ (high spin, h_s) which is a Jahn-Teller ion and which distorts the unit cell to larger sizes.⁹ If multiple valence states of Mn are present, the film can decrease the lattice distortion that would be caused by Mn³⁺ alone, which may result in better lattice matching between the film and the substrate. Other possibilities such as film defects may also have played an important role in changing the valence states of Mn.

B. Electronic structures and effect of U

To investigate the electronic structure of BiFeO₃, BiMnO₃ and Bi₂FeMnO₆, we also carried out calculations on the den-

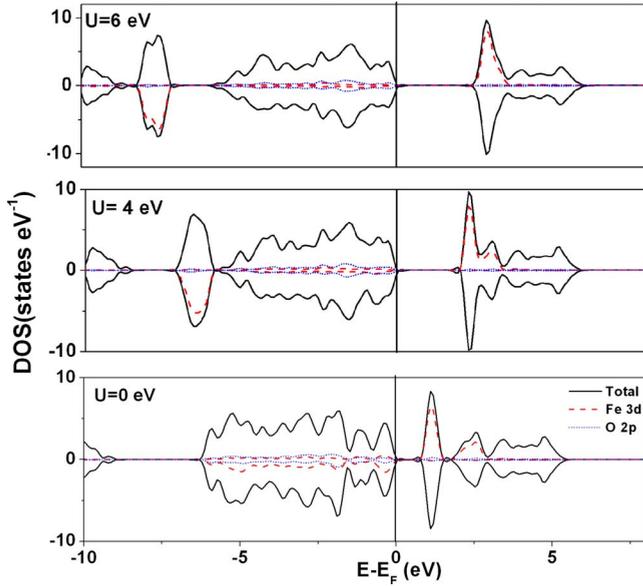


FIG. 7. (Color online) Total, Fe 3d and O 2p DOS for R3c-structured BiFeO₃ calculated using GGA method ($U=J=0$ eV) and GGA+ U method ($J=1$ eV, $U=5$ eV and $J=1$ eV $U=7$ eV). The total DOS is normalized to a formula unit of Bi₂Fe₂O₆. As U increases, the calculated band-gap energy increases, and the ionicity of Fe-O bonds increases.

sity of states (DOS) of these compounds. Figure 7 shows the calculated DOS for both spin channels of R3c BiFeO₃ using various U values. In all three calculations, BiFeO₃ is predicted to be an insulator. The band gaps are 0.4 eV, 2 eV and 2.4 eV for $U=0$ eV, 5 eV and 7 eV, respectively. Increasing the U value significantly increases the band gap, and $U=7$ eV shows the band-gap value closest to our experimental values. Changing the U value also influences the ionicity of the Fe-O bonding. For $U=0$ eV, Fe 3d and O 2p valence electrons show strong hybridization in the energy range of -6 to 0 eV, indicating the Fe-O bonding is highly covalent. This is not reasonable if we consider the electronegativity is quite different between Fe (1.83) and O (3.44). However, as the U value increases, Fe 3d valence electrons are pushed down to lower energy levels, and the $t_{2g}-e_g$ energy split is smaller. This indicates that the Fe-O bonding is more ionic and the electrons are more localized on the Fe and O atoms. Electron spin integration around the Fe site shows that the magnetic moment of Fe is 3.75 μ_B , 4.13 μ_B and 4.25 μ_B for $U=0$ eV, 5 eV and 7 eV, respectively. Interestingly, $U=0$ eV rather than $U=7$ eV provides the best prediction of Fe magnetic moment compared with experiments.⁴⁴ These calculation results using the GGA+ U method are similar to previous results calculated by local spin-density approximation (LSDA) and LSDA+ U methods.¹⁷ The difference is that for the same U value, GGA predicts slightly larger band gaps and Fe magnetic moments compared with LSDA.

Figure 8 shows the calculated DOS of C2 BiMnO₃ for both spin channels using the GGA+ U method ($U=0, 6$, and 8 eV). For insulating BiMnO₃, it is well known that the LSDA method predicts a half-metallic band structure.^{9,45,46} This is due to the strong hybridization tendency between Mn 3d and O 2p orbitals in first-principles calculations. Our

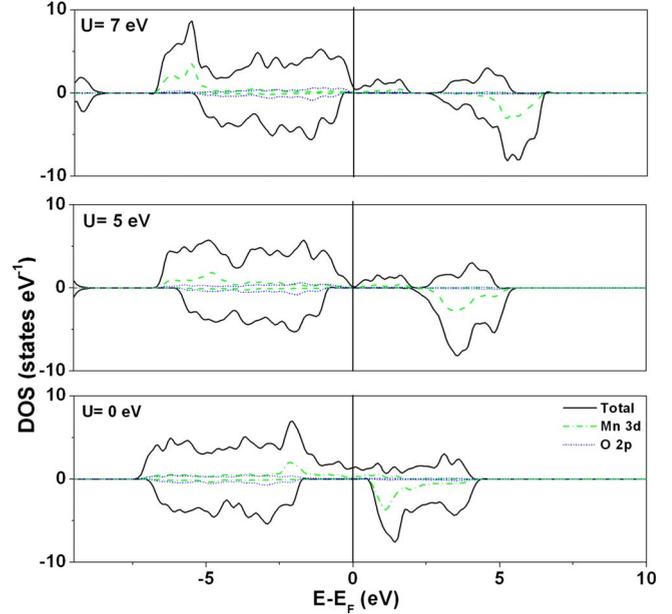


FIG. 8. (Color online) Total, Fe 3d and O 2p DOS for C2 BiMnO₃ calculated using GGA method ($U=J=0$ eV) and GGA+ U method ($J=1$ eV, $U=6$ eV and $J=1$ eV, $U=8$ eV). The total DOS is normalized to a formula unit of Bi₂Mn₂O₆.

calculation based on monoclinic BiMnO₃ using the GGA method also shows similar behavior. When $U=0$ eV, Mn 3d and O 2p electrons strongly hybridize and there is no band gap. Applying the GGA+ U method enhances the ionicity of the Mn-O bonding and creates a dip in the DOS near the Fermi energy level. A gap of about 0.4 eV opens between the occupied and unoccupied Mn e_g^\uparrow states. This effect was observed by Shishidou *et al.*⁴⁶ using LDA+ U calculations. Unlike BiFeO₃, as we increase the U value up to 8 eV, this gap does not increase.

However, applying GGA or GGA+ U methods to calculate the electronic structure of C2 Bi₂FeMnO₆ shows dramatic differences compared with BiMnO₃. Figures 9(a) and 9(b) show the calculated DOS of monoclinic Bi₂FeMnO₆ with antiferromagnetic spin ordering by applying GGA and GGA+ U methods ($U(\text{Fe})=7$ eV, $U(\text{Mn})=6$ eV), respectively. The GGA method predicts Bi₂FeMnO₆ to be half metallic, while GGA+ U indicates Bi₂FeMnO₆ should be insulating. Compared with our optical measurements, it is clear that the GGA+ U method provides a more realistic result. Looking closely into the details of the density of states, the 100% spin polarized structure in the GGA calculation is due to the hybridization of Fe 3d, O 2p, and Mn 3d orbitals. The unoccupied Mn e_g^\downarrow states hybridize with Fe t_{2g}^\downarrow and e_g^\downarrow states through oxygen, causing a half-metallic structure. In the GGA+ U method, the Coulomb repulsion and correlation interaction correction causes lower hybridization between Fe and Mn orbitals, and a gap opens above the Fermi level. Despite this, hybridized states among Fe 3d, Mn 3d, and O 2p orbitals can still be found in the valence and conduction bands. This result predicts that Mn-O-Fe type hopping conduction is likely to take place in Bi₂FeMnO₆.

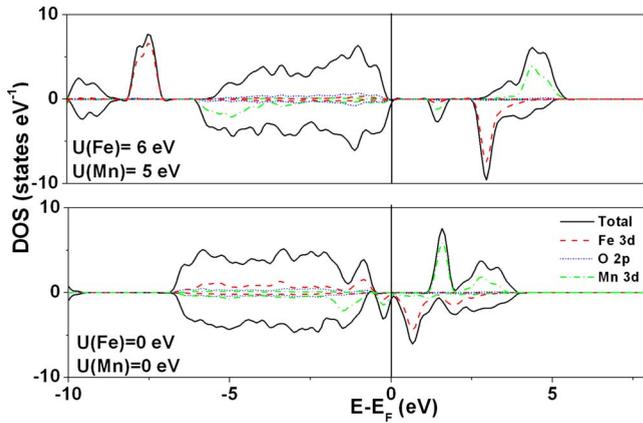


FIG. 9. (Color online) Total, Fe 3d and O 2p DOS for $C2$ $\text{Bi}_2\text{FeMnO}_6$ calculated using GGA method ($J(\text{Fe})=J(\text{Mn})=0$ eV, $U(\text{Fe})=U(\text{Mn})=0$ eV) and GGA+ U method ($J(\text{Fe})=1$ eV, $U(\text{Fe})=7$ eV and $J(\text{Mn})=1$ eV, $U(\text{Mn})=6$ eV). The total DOS is normalized to a formula unit of $\text{Bi}_2\text{FeMnO}_6$. The GGA method predicts a half-metallic band structure while GGA+ U indicates this material should be insulating.

VI. DISCUSSION

It is now useful to compare our experimental results and calculations to understand the properties of $\text{Bi}_2\text{FeMnO}_6$. The formation enthalpy for bulk ordered $\text{Bi}_2\text{FeMnO}_6$ is predicted to be positive for several crystal symmetries by density-functional theory, which assumes equilibrium phases and atmospheric pressure. This suggests that neighboring Fe and Mn octahedra are not thermodynamically favored in this material; thus it could be difficult to fabricate it as an ordered bulk material. This observation is evident in one previous study by Yang *et al.*,⁴⁷ who claimed that incorporating Mn >30 at. % on the B site of BiFeO_3 is difficult unless high pressure processing is used. Experimentally, the smaller process window for forming $\text{Bi}_2\text{FeMnO}_6$ as compared to BiFeO_3 (the oxygen pressure window for BiFeO_3 growth exceeds 4.5 mTorr while for $\text{Bi}_2\text{FeMnO}_6$ it is smaller than 0.4 mTorr) may be indicative of the relative instability of the $\text{Bi}_2\text{FeMnO}_6$ perovskite phase, and our films showed no evidence of B -site ordering. In contrast, there are several ordered double perovskites that can be grown by bulk processing, such as $\text{La}_2\text{MnNiO}_6$,⁴⁸ $\text{La}_2\text{MnCoO}_6$,⁴⁹ and $\text{Sr}_2\text{FeMoO}_6$,⁵⁰ and it will be interesting to investigate whether a negative formation enthalpy is predicted in these ordered perovskites following the computational methods used here.

We observed experimentally that Mn tends to adopt multiple valence states in the perovskite film. From the calculation results we infer that Mn^{3+} is thermodynamically the most stable ion in $\text{Bi}_2\text{FeMnO}_6$. One possible explanation of the experimental observation is that by Mn adopting multiple valence states, the material can reduce the Jahn-Teller effect from Mn^{3+} . For a thin-film material, this process may pro-

mote better lattice matching with the substrate, lowering the interface and strain energies. Other factors such as film defects may also affect the valence states of Mn.

In $\text{Bi}_2\text{FeMnO}_6$, the electronic structure calculation predicts a strong tendency for Fe-O-Mn hybridization, and the resulting conductivity due to interatomic hopping is expected to be higher than the conductivity of BiFeO_3 . The optical absorption spectrum may provide some insight into the conductivity. The large absorption of $\text{Bi}_2\text{FeMnO}_6$ in the infrared may be due to free-carrier absorption. The absorption peak around 1100 nm does not correspond to any dipole transition energies of Fe or Mn sites, and may therefore be due to interatomic electron hopping, i.e., Verwey conduction. In addition, hopping conduction between Mn with different valence states is possible, as observed for example in $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ perovskite.⁵¹ This requires significant amounts of Mn^{2+} and Mn^{4+} to allow percolation to take place. Quantitative analysis on the amount of Mn^{2+} and Mn^{4+} ions may provide more information on the importance of these two conduction mechanisms. The relatively high conductivity of polycrystalline $\text{Bi}_2\text{FeMnO}_6$ was shown in one previous study, although grain-boundary conduction and the effects of secondary phases may have been important.⁵²

VII. CONCLUSIONS

The structure, magnetic, and magneto-optical properties of BiFeO_3 and $\text{Bi}_2\text{FeMnO}_6$ have been investigated using both experimental and first-principles methods. Both BiFeO_3 and $\text{Bi}_2\text{FeMnO}_6$ can be epitaxially grown in the perovskite structure on SrTiO_3 (001) substrates within a small window of process parameters. Compared with BiFeO_3 , $\text{Bi}_2\text{FeMnO}_6$ shows a smaller process window, and its magnetic properties imply that the B -site cations are disordered. These observations are attributed to the positive formation enthalpy of ordered $\text{Bi}_2\text{FeMnO}_6$ compared with BiFeO_3 and BiMnO_3 at 0 K. Mn tends to form multiple valence states in $\text{Bi}_2\text{FeMnO}_6$ despite the higher stability of the compound only containing Mn^{3+} ions, possibly because the incorporation of Mn^{2+} or Mn^{4+} decreases the Jahn-Teller effect of Mn^{3+} in the film. $\text{Bi}_2\text{FeMnO}_6$ had a large optical absorption compared to BiMnO_3 as a result of electron hopping between Fe and Mn sites as well as between Mn sites with different valence states. These studies provide a comparison between the structure and properties of BiFeO_3 perovskite and $\text{Bi}_2\text{FeMnO}_6$ double perovskite which may be applicable to other perovskite and multiferroic systems.

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- *Also at MIT Lincoln Laboratory Lexington, Massachusetts, 02420.
- ¹P. Baettig, C. Ederer, and N. A. Spaldin, *Phys. Rev. B* **72**, 214105 (2005).
 - ²M. Azuma, K. Takata, T. Saito, S. Ishiwata, Y. Shimawaka, and M. Takano, *J. Am. Chem. Soc.* **127**, 8889 (2005).
 - ³R. Nechache, C. Harnage, A. Pignolet, F. Normandin, T. Veres, L. Carignan, and D. Ménard, *Appl. Phys. Lett.* **89**, 102902 (2006).
 - ⁴X. Tan, R. Wongmanerung, and R. W. McCallum, *J. Appl. Phys.* **102**, 104114 (2007).
 - ⁵S. Yasui, H. Uchida, H. Nakaki, K. Nishida, H. Funakubo, and S. Koda, *Appl. Phys. Lett.* **91**, 022906 (2007).
 - ⁶N. A. Hill, *J. Phys. Chem. B* **104**, 6694 (2000).
 - ⁷G. A. Smolenskii and I. Chupis, *Sov. Phys. Usp.* **25**, 475 (1982).
 - ⁸N. A. Spaldin and M. Fiebig, *Science* **309**, 391 (2005).
 - ⁹R. Seshadri and N. A. Hill, *Chem. Mater.* **13**, 2892 (2001).
 - ¹⁰M. Levy, *IEEE J. Sel. Top. Quantum Electron.* **8**, 1300 (2002).
 - ¹¹D. C. Hutchings, *J. Phys. D* **36**, 2222 (2003).
 - ¹²G. F. Dionne, A. R. Taussig, M. Bolduc, L. Bi, and C. A. Ross, *J. Appl. Phys.* **101**, 09C524 (2007).
 - ¹³G. F. Dionne and G. A. Allen, *J. Appl. Phys.* **73**, 6127 (1993).
 - ¹⁴G. F. Dionne and G. A. Allen, *J. Appl. Phys.* **75**, 6372 (1994).
 - ¹⁵H. Bea, M. Bibes, A. Barthelémy, K. Bouzouane, E. Jacquet, A. Khodan, J.-P. Contour, S. Fusil, F. Wyczisk, A. Forget, D. Lebeugle, D. Colson, and M. Viret, *Appl. Phys. Lett.* **87**, 072508 (2005).
 - ¹⁶J. Li, J. Wang, M. Wuttig, R. Ramesh, N. Wang, B. Ruetter, A. P. Pyatakov, A. K. Zvezdin, and D. Viehland, *Appl. Phys. Lett.* **84**, 5261 (2004).
 - ¹⁷J. B. Neaton, C. Ederer, U. V. Waghmare, N. A. Spaldin, and K. M. Rabe, *Phys. Rev. B* **71**, 014113 (2005).
 - ¹⁸J. Wang, Ph.D. thesis, University of Maryland, 2005.
 - ¹⁹S. V. Kiselev, R. P. Ozerov, and G. S. Zhdanov, *Sov. Phys. Dokl.* **7**, 742 (1963).
 - ²⁰J. R. Teague, R. Gerson, and W. J. James, *Solid State Commun.* **8**, 1073 (1970).
 - ²¹B. Ruetter, S. Zvyagin, A. P. Pyatakov, A. Bush, J. F. Li, V. I. Belotelov, A. K. Zvezdin, and D. Viehland, *Phys. Rev. B* **69**, 064114 (2004).
 - ²²A. Sharan, J. Lettieri, Y. Jia, W. Tian, X. Pan, D. G. Schlom, and V. Gopalan, *Phys. Rev. B* **69**, 214109 (2004).
 - ²³T. Kimura, S. Kawamoto, I. Yamada, M. Azuma, M. Takano, and Y. Tokura, *Phys. Rev. B* **67**, 180401(R) (2003).
 - ²⁴A. Moreira dos Santos, S. Parashar, A. R. Raju, Y. S. Zhao, A. K. Cheetham, and C. N. R. Rao, *Solid State Commun.* **122**, 49 (2002).
 - ²⁵J. B. Goodenough, *Magnetism and the Chemical Bond* (Wiley, New York, 1963), Table XII.
 - ²⁶J. B. Goodenough, A. Wold, N. Menyuk, and R. J. Arnett, *Phys. Rev.* **124**, 373 (1961).
 - ²⁷G. F. Dionne, *J. Appl. Phys.* **79**, 5172 (1996).
 - ²⁸C. H. Yang, J. H. Song, H. J. Lee, S. Yoon, T. Y. Koo, and Y. H. Jeong, *Phys. Status Solidi B* **241**, 1453 (2004).
 - ²⁹D. Kothari, V. R. Reddy, A. Gupta, D. M. Phase, N. Lakshmi, S. K. Deshpande, and A. M. Awasthi, *J. Phys.: Condens. Matter* **19**, 136202 (2007).
 - ³⁰J. R. Sahu and C. N. R. Rao, *Solid State Sci.* **9**, 950 (2007).
 - ³¹V. R. Palkar, D. C. Kundaliya, and S. K. Malik, *J. Appl. Phys.* **93**, 4337 (2003).
 - ³²D. L. Wood, J. P. Remeika, and E. D. Kolb, *J. Appl. Phys.* **41**, 13 (1970).
 - ³³W. J. Tabor, A. W. Anderson, and L. G. Van Uitert, *J. Appl. Phys.* **41**, 3018 (1970).
 - ³⁴G. F. Dionne and G. A. Allen, *J. Appl. Phys.* **95**, 7333 (2004).
 - ³⁵B. B. He, *Powder Diffr.* **18**, 71 (2003).
 - ³⁶A. Rajamani, G. F. Dionne, D. Bono, and C. A. Ross, *J. Appl. Phys.* **98**, 063907 (2005).
 - ³⁷H. Béa, M. Bibes, S. Fusil, K. Bouzouane, E. Jacquet, K. Rode, P. Bencok, and A. Barthelémy, *Phys. Rev. B* **74**, 020101(R) (2006).
 - ³⁸C. Wandelt, *Surf. Sci. Rep.* **2**, 1 (1982).
 - ³⁹A. I. Liechtenstein, V. I. Anisimov, and J. Zaanen, *Phys. Rev. B* **52**, R5467 (1995).
 - ⁴⁰G. Kresse and D. Joubert, *Phys. Rev. B* **59**, 1758 (1999).
 - ⁴¹G. Kresse and J. Furthmüller, *Phys. Rev. B* **54**, 11169 (1996).
 - ⁴²F. Kubel and H. Schmid, *Acta Crystallogr., Sect. B: Struct. Sci.* **46**, 698 (1990).
 - ⁴³T. Atou, H. Chiba, K. Ohoyama, Y. Yamaguchi, and Y. Syono, *J. Solid State Chem.* **145**, 639 (1999).
 - ⁴⁴I. Sosnowska, W. Schäfer, W. Kockelmann, K. H. Andersen, and I. O. Troyanchuk, *Appl. Phys. A: Mater. Sci. Process.* **74**, S1040 (2002).
 - ⁴⁵N. A. Hill and K. M. Rabe, *Phys. Rev. B* **59**, 8759 (1999).
 - ⁴⁶T. Shishidou, N. Mikamo, Y. Uratani, F. Ishii, and T. Oguchil, *J. Phys.: Condens. Matter* **16**, S5677 (2004).
 - ⁴⁷C. H. Yang, T. Y. Koo, and Y. H. Jeong, *Solid State Commun.* **134**, 299 (2005).
 - ⁴⁸N. S. Rogado, J. Li, A. W. Sleight, and M. A. Subramanian, *Adv. Mater. (Weinheim, Ger.)* **17**, 2225 (2005).
 - ⁴⁹C. L. Bull, D. Gleeson, and K. S. Knight, *J. Phys.: Condens. Matter* **15**, 4927 (2003).
 - ⁵⁰K. I. Kobayashi, T. Kimura, H. Sawada, K. Terakura, and Y. Tokura, *Nature (London)* **395**, 677 (1998).
 - ⁵¹M. Izumi, T. Manako, Y. Konishi, M. Kawasaki, and Y. Tokura, *Phys. Rev. B* **61**, 12187 (2000).
 - ⁵²S. K. Singh, H. Ishiwara, and K. Maruyama, *Appl. Phys. Lett.* **88**, 262908 (2006).